

Basic Information: The Book Class Conceptualized out of 7th (5th?) Edition		Basic Information: Syllabus
<text></text>	Title: "Numerical Analysis," 9th Edition (older OK) Authors: Richard L. Burden & J. Douglas Faires Publisher: Brooks/Cole CENGAGE Learning ISBN-10: 0-534-73351-9	ChapterTitle1Mathematical Preliminaries2Solutions of Equations in One Variable3Interpolation and Polynomial Approximation4Numerical Differentiation and Integration6Direct Methods for Solving Linear Systems8Approximation TheoryMath 542:Numerical Solutions of Differential Equations5Initial-Value Problems for ODEs11Boundary Value Problems for ODEs11Boundary Value Problems for ODEs7Iterative Techniques in Matrix Algebra9Approximating EigenvaluesMath 693a:Advanced Numerical Analysis (Numerical Optimization)10Numerical Solution of Nonlinear Systems of Equations12Numerical Solution of PDEs
	Lecture Notes #1 — First Meeting — (9/33)	Lecture Notes #1 — First Meeting — (10/33)
Recent (and Growing) Influence c	n the Class	Basic Information: Grading
<text></text>	Title:"Approximation Theory and Approximation Practice,"Author:Lloyd N. TrefethenPublisher:SIAMISBN:978-1-611972-39-9	 Homework* 25% Midterm #1+ 25% Midterm #2+ 25% Final× 25% * There will be ≈8 homework assignments; they will be posted and submitted thru http://webwork.sdsu.edu/ + The midterms(s) may be take-home (target date(s): week #6, week #11.) × Scheduled time: Tuesday, Dec 16, 1:00pm-3:00pm. (Details to be determined.)
	Lecture Notes #1 — First Meeting — (11/33)	Lecture Notes $\#1 - First$ Meeting $-(12/33)$

Homework \sim Webwork	Homework \sim Webwork		
 "WeBWorK is a web-based interactive system designed to make homework in mathematics and the sciences more effective and efficient." Info resource http://webwork.maa.org/wiki/Category:Students Homeworks will "open" (on http://webwork.sdsu.edu/), on the first day material relevant to the HW is covered in class. Homeworks will "close" (be due), no less than 8 days after the last material relevant to the HW is covered in class. Your Lastname is your LoginID, and RedID is your initial password. If your Lastname is not unique, then your loginID is Lastname+Firstname-initial. 	 Most HW problems involve both a theoretical, and implementation (programming) part — Matlab is the recommended and supported environment, but feel free to program in 6510 assembler, Java, Fortran, C/C++, M\$-D^b You will enter specific results from your code into Webwork. Some assignments may require additional hardcopy submissions; read the webwork instructions. Start Assignments EARLY. Sometimes "interesting" things happen in Webwork (which does computations using Perl), which make Webwork computations different from Matlab computations. 		
Lecture Notes #1 — First Meeting — (13/33)	Lecture Notes #1 — First Meeting — (14/33)		
Expectations and Procedures, I	 Expectations and Procedures, II Please, turn in assignments on time. (The instructor reserves 		
 Most class attendance is "OPTIONAL" — Homework and announcements will be posted on the class web page. If/when you attend class: Please be on time. Please pay attention. Please turn off mobile phones. 	 the right not to accept late assignments.) The instructor will make special arrangements for students with documented learning disabilities and will try to make accommodations for other unforeseen circumstances, <i>e.g.</i> illness, personal/family crises, etc. in a way that is fair to all students enrolled in the class. Please contact the instructor EARLY regarding special circumstances. 		
 Please be courteous to other students and the instructor. Abide by university statutes, and all applicable local, state, and federal laws. 	 Students are expected and encouraged to ask questions in class! Students are expected and encouraged to to make use of office hours! If you cannot make it to the scheduled office hours: contact the instructor to schedule an appointment! 		
Lecture Notes $\#1$ — First Meeting — (15/33)	Lecture Notes #1 — First Meeting — (16/33)		

Expectations and Procedures, III	Honesty Pledges, I		
 Missed midterm exams: Don't miss exams! The instructor reserves the right to schedule make-up exams, make such exams oral presentation, and/or base the grade solely on other work (including the final exam). Missed final exam: Don't miss the final! Contact the instructor ASAP or a grade of WU or F will be assigned. Academic honesty: submit your own work — but feel free to discuss homework with other students in the class! It's OK to ask "Uncle Google" and "Aunt Wiki" for help and ideas, but process the information and make it your own, AND cite any and all sources you use. 	 The following Honesty Pledge must be included in all programs you submit (as part of homework and/or projects): I, (your name), pledge that this program is completely my own work, and that I did not take, borrow or steal code from any other person, and that I did not allow any other person to use, have, borrow or steal portions of my code. I understand that if I violate this honesty pledge, I am subject to disciplinary action pursuant to the appropriate sections of the San Diego State University Policies. Work missing the honesty pledge may not be graded! 		
Lecture Notes #1 — First Meeting — (17/33)	Lecture Notes #1 — First Meeting — (18/33)		
 Honesty Pledges, II Larger reports must contain the following text: I, (your name), pledge that this report is completely my own 	 Computer Resources Access to a (somewhat) current release of Matlab is highly recommended. The GMCS-422/428 labs will be available. 		
 work, and that I did not take, borrow or steal any portions from any other person. Any and all references I used are clearly cited in the text. I understand that if I violate this honesty pledge, I am subject to disciplinary action pursuant to the appropriate sections of the San Diego State University Policies. Your signature. Work missing the honesty pledge may not be graded! 	 You can also use the Rohan Sun Enterprise system or another capable system. How to open a ROHAN account: http://www-rohan.sdsu.edu/raccts.shtml You may also want to consider buying the student version of Matlab: http://www.mathworks.com/ SDSU students can download a copy of matlab from http://www-rohan.sdsu.edu/~download/matlab.html 		

Lecture Notes #1 — First Meeting

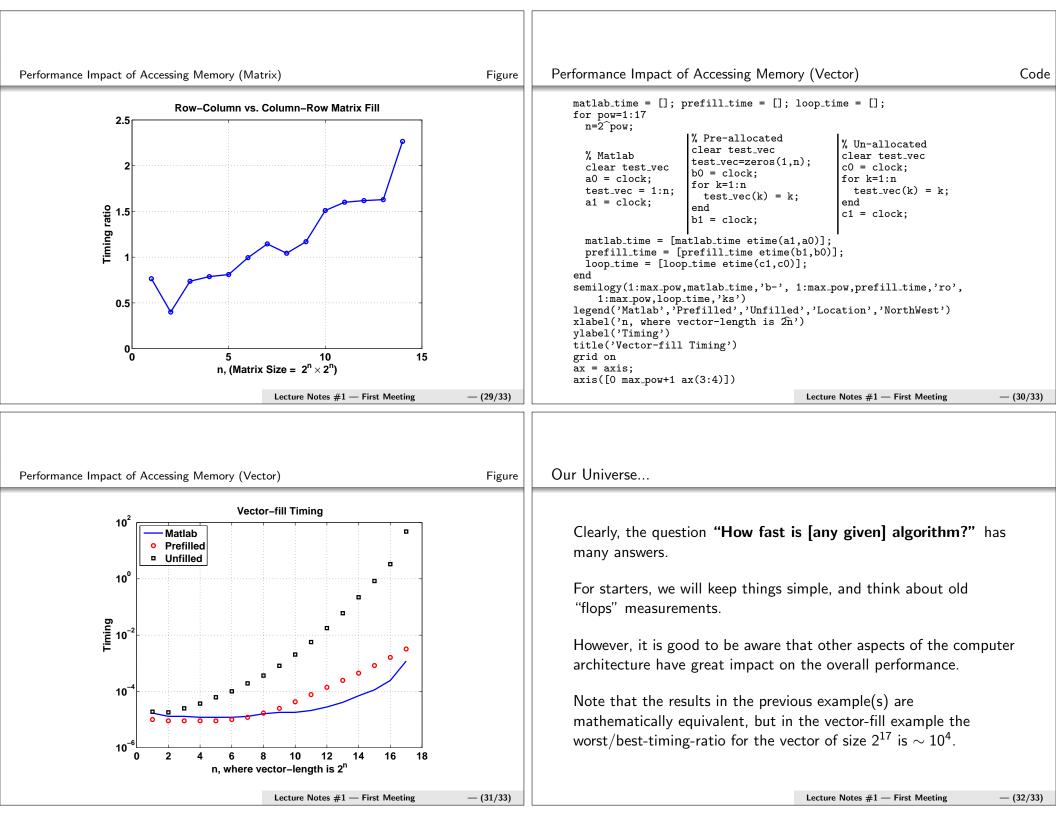
— (20/33)

Math 541: Formal Prerequisites I of II		Math 541: Formal Prerequisites II of II		
 Math 541: Formal Prerequisites Math 254, or Math 342A 254 ⇒ Introduction to Linear Algebra Matrix Algebra, Gaussian elimination, determinants, vector spaces, linear transformations, orthogonality, eigenvalues and eigenvectors. 342A ⇒ Methods of Applied Mathematics, I Vector analysis, divergence and Stokes' theorem, integral theorems. Matrix analysis, eigenvalues and eigenvectors, diagonalization. Introduction to ODEs. Computer software for matrix applications, solving, and graphing differential equations. 		Math 541: Formal Prerequisites II of II CS 106, CS 107 or CS 205 106 ⇒ Intro to Programming: FORTRAN • Problem solving using a computer, design of algorithms. 107 ⇒ Intro to Programming: JAVA • Programming methodology and problem solving. Basic concepts of computer systems, algorithm design and development, data types, program structures. 205 ⇒ Intro to Programming and Visualization • Problem solving skills for science, computing/software tools of computational science, computer communications, programming and visualization.		
	Lecture Notes #1 — First Meeting — (21/33)	Lecture Notes #1 — First Meeting — (22/33)		
Math 541: Introduction –	– What we will learn	Math 541: Introduction — Why???		
• Numerical tools for	or problem solving:	Q: Why are numerical methods needed?		
	Newton's Method for $f(x) = 0$. Least squares approximation.	A: To accurately approximate the solutions of problems that cannot be solved exactly.		
$\Rightarrow \texttt{powertool}$	The Fast Fourier Transform (FFT).	Q: What kind of applications can benefit from numerical studies?		
	Polynomial Interpolation.	A: Engineering, physics, chemistry, computer, biological and so- cial sciences.		
\Rightarrow foundation	Numerical differentiation and integration. Taylor's Theorem. Weierstrass' Theorem.	Image processing / computer vision, computer graphics (ren- dering, animation), climate modeling, weather predictions, "virtual" crash-testing of cars, medical imaging ($CT = Com-$ puted Tomography), AIDS research (virus decay vs. medica- tion), financial math		
	Lecture Notes #1 — First Meeting — (23/33)	Lecture Notes #1 — First Meeting — (24/33)		

Computing: Historical Perspective...

The Apollo Guidance Computer (1969)Word Length15 bits plus parityFixed Memory Registers $36,864$ WordsErasable Memory Registers $2,048$ WordsNumber of Normal Instructions 34 Number of Involuntary Instructions 10 Number of Interface Circuits 227 Memory Cycle time $11.7 \mu s$ ($85 \mathrm{kHz}$)Addition Time $23.4 \mu s$ Multiplication Time $46.8 \mu s$ Number of Logic Gates $5,600$ ($2,800 \mathrm{packages}$)Volume $0.97 \mathrm{cubic feet}$ Weight70 \mathrm{pounds}Power Consumption $55 \mathrm{watts}$		We need some measure of how fast, or slow, an algorithm is (independent of the computational architecture) In the old-old days multiplications (and divisions) where a lot slower additions (and subtractions) $T_{*,/} \gg T_{+,-}$; so one would count the number of multiplications (see <i>e.g.</i> the timings for the Apollo guidance computer.) Then chip designers figured out how to make multiplications faster, so $T_{*,/} \approx T_{+,-}$, so in the old days one would count all operations. Yesterday, processors where so fast that memory accesses dominated the processing time; in particular cache-misses , so we end up with a completely different model			
	cture Notes $\#1$ — First Meeting	— (25/33)		Lecture Notes #1 — First Meeting	— (26/33)
Counting Work: The Memory Access Latency Model If we have three cache-levels (L1, L2, and L3), some average hit-rate (and hence miss-rate) for each level and the time it takes to access that cache-level (the hit-cycle-time), then we end up with a measure for the average memory access latency per memory access $T \sim (L1_hit_rate * L1_hit_cycle_time)$ $+ (L1_miss_L2_hit_rate * L2_hit_cycle_time)$ $+ (L2_miss_L3_hit_rate * L3_hit_cycle_time)$ $+ (L3_miss_rate * [S]DRAM_latency)$ If this does not scare you, please get a Ph.D. in algorithm design on the compiler / silicon level!!! Meanwhile, the rest of us will count "flops", <i>i.e.</i> floating-point operations (multiplications and additions)!			<pre>Performance Impact of Accessing Mem for pow=1:14 n=2`pow; clear A A = zeros(n,n); a0 = clock; for c=1:n for r=1:n A(r,c) = 1/(1+r+c); end a1 = clock; a.time = [a.time etime(a1,a0)]; b.time = [b.time etime(b1,b0)]; end plot((1:14),b.time./a.time,'o-') ax = axis; axis([0 15 ax(3:4)]) grid on xlabel('n, (Matrix Size = 2`n × 2`) ylabel('Timing ratio') title('Row-Column vs. Column-Row Merice </pre>	<pre>clear B B = zeros(n,n); b0 = clock; for r=1:n for c=1:n B(r,c) = 1/(1+r+c); end b1 = clock;</pre>	Matlab Code

Counting Work: Ancient, Old, and Somewhat Recent Measures





- $\bullet \ \texttt{http://terminus.sdsu.edu/SDSU/Math541_f2014/}$
 - The Class website
- http://webwork.sdsu.edu/
 - Webwork server, for homework.
- http://webwork.maa.org/wiki/Category:Students
 - $\bullet\,$ Some information about Webwork
- http://www-rohan.sdsu.edu/raccts.shtml
 - "Obtaining a ROHAN Computer Account"
- http://www.mathworks.com/
 - Mathworks, the makers of Matlab
- http://www-rohan.sdsu.edu/~download/matlab.html
 - On-campus matlab download.

Lecture Notes #1 — First Meeting — (33/33)